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BaBar  $|V_{xb}|$  and  $|V_{tx}|$  workshop  
SLAC, December, 4–6 2002

# $B \rightarrow K^* \gamma$ and $B \rightarrow \rho \gamma$ at NLO from QCD Factorization

in collaboration with Gerhard Buchalla

- I. Introduction
- II. Basic Formulas
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- IV. Summary

# Introduction

radiative FCNC  $b \rightarrow s (d) \gamma$  transition

- high sensitivity to **New Physics**
- **large** impact of **SD QCD corrections**
- **experimentally accessible** already at present

**inclusive** mode

- $B(B \rightarrow X_s \gamma)_{exp} = (3.41 \pm 0.36) \cdot 10^{-4}$   
ALEPH, BABAR, BELLE, CLEO
- **HQE**  $\rightarrow$  **perturbative** calculation Adel, Yao  
Chetyrkin, Misiak, Münz  
Greub, Hurth, Wyler

**exclusive** mode

- $B(B^0 \rightarrow K^{*0} \gamma)_{exp} = (4.59 \pm 0.55) \cdot 10^{-5}$   
 $B(B^+ \rightarrow K^{*+} \gamma)_{exp} = (3.82 \pm 0.78) \cdot 10^{-5}$   
 $B(B^0 \rightarrow \rho^0 \gamma)_{exp} < 1.5 \cdot 10^{-6}$  at 90% C.L.  
 $B(B^+ \rightarrow \rho^+ \gamma)_{exp} < 2.8 \cdot 10^{-6}$   
CLEO, BELLE, BABAR
- bound state effects essential
  - $\rightarrow$  **nonperturbative** hadronic form-factors
  - $\rightarrow$  **QCD factorization**  
Beneke, Buchalla, Neubert, Sachrajda
  - $\rightarrow$  **systematic** model-independent **NLL** framework  
Beneke, Feldmann, Seidel  
SWB, Buchalla

# Basic Formulas for $B \rightarrow V \gamma$

Beneke, Feldmann, Seidel  
Ali, Parkhomenko  
SWB, Buchalla

$$\mathcal{H}_{eff} = \frac{G_F}{\sqrt{2}} \sum_{p,i} \lambda_p^{CKM} C_i(\mu) Q_i^p$$

$$Q_{CC}^p = (\bar{s} p)_{V-A} (\bar{p} b)_{V-A}$$

$$Q_{pen} = (\bar{s} p)_{V-A} \sum_q (\bar{q} q)_{V \mp A}$$

$$Q_7 = \frac{e}{8\pi^2} m_b \bar{s} \sigma^{\mu\nu} (1 + \gamma_5) b F_{\mu\nu}$$

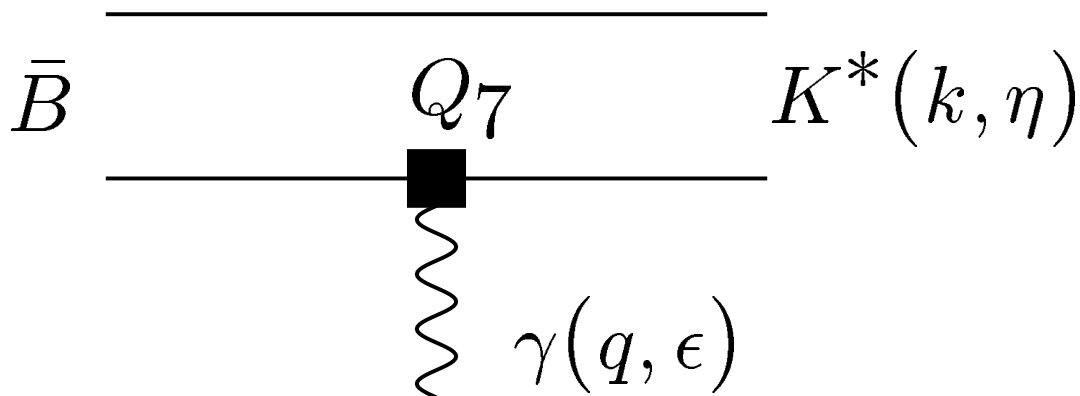
$$Q_8 = \frac{g}{8\pi^2} m_b \bar{s} \sigma^{\mu\nu} (1 + \gamma_5) T^a b G_{\mu\nu}^a$$

matrix elements  $\langle V \gamma(\epsilon) | Q_i | \bar{B} \rangle$  in heavy quark limit  $m_b \gg \Lambda_{QCD} \rightarrow$  factorization formula in l.d.g. power

$$\langle Q_i \rangle = \left[ F^{B \rightarrow V} T_i^I + \int_0^1 d\xi dv T_i^{II}(\xi, v) \Phi_B(\xi) \Phi_V(v) \right] \cdot \epsilon$$

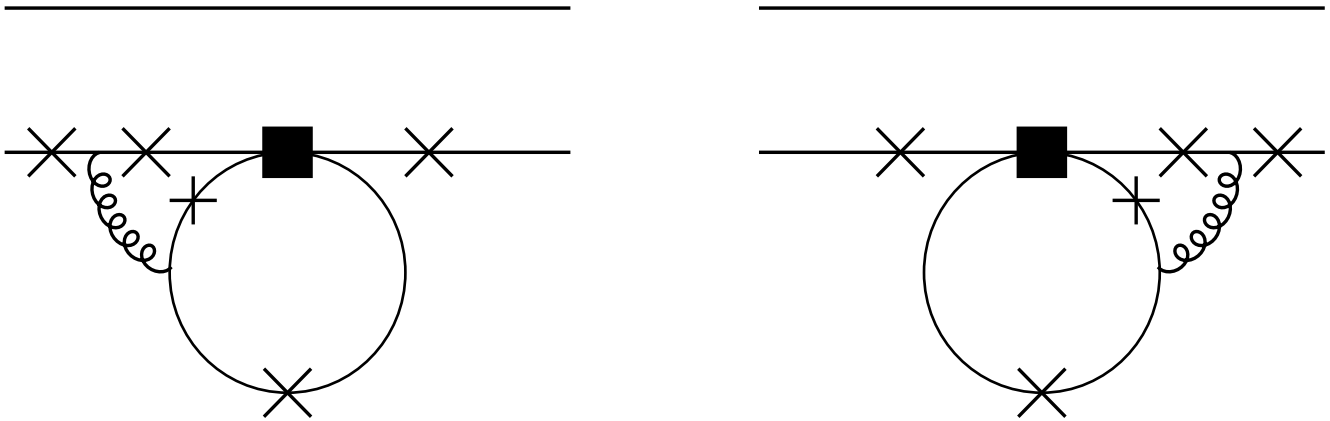
universal nonperturbative form factor and LCDAs factorized from perturbative hard-scattering kernels

LO contribution from  $Q_7$



$$\langle Q_7 \rangle = \frac{-e}{2\pi^2} m_b F_V [\varepsilon(\epsilon, \eta, k, q) + i(\epsilon \cdot \eta k \cdot q - \epsilon \cdot k \eta \cdot q)]$$

# NLO type I

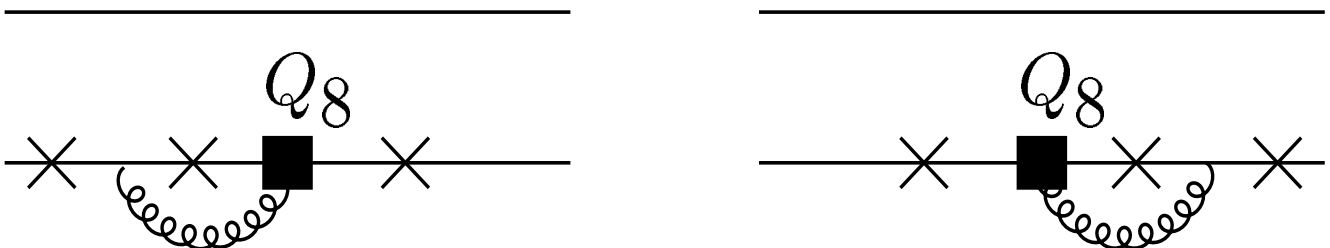


$$\langle Q_i \rangle^I = \langle Q_7 \rangle \frac{\alpha_s C_F}{4\pi} G_i$$

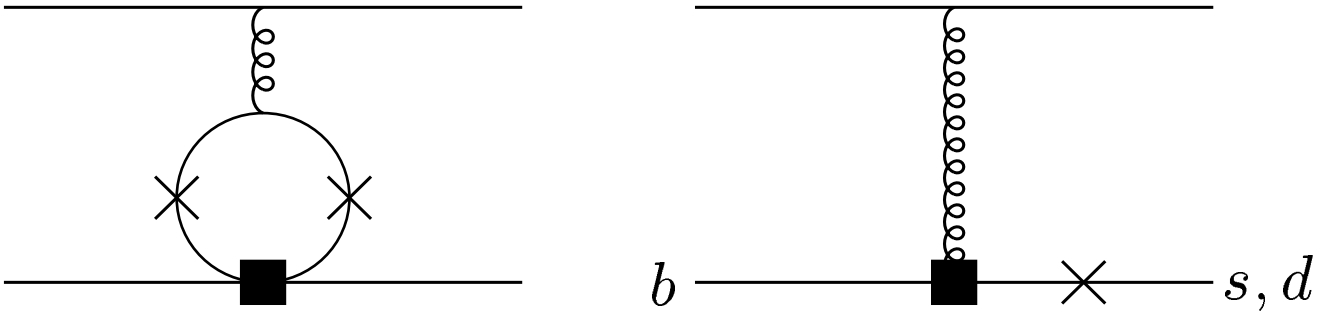
$$G_i(s_c) = l_i \ln \frac{\mu}{m_b} + g_i(s_c) \underbrace{= m_c^2 / m_b^2}$$

Greub, Hurth, Wyler  
Buras, Czarnecki, Misiak, Urban

Dominated by hard scales  $\sim m_b \rightarrow$  IR finite

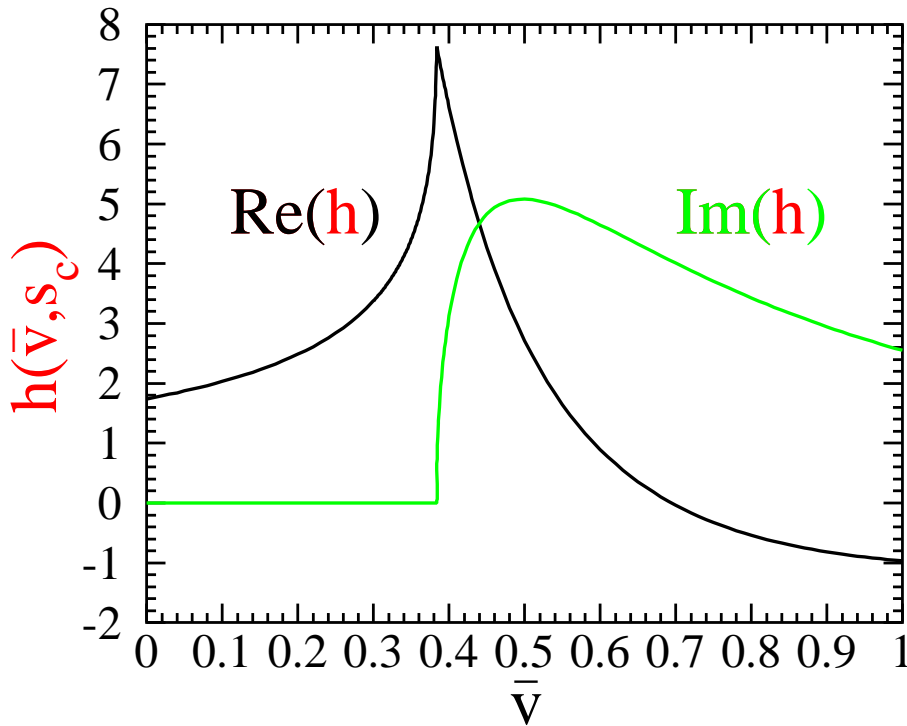


# NLO type II



$$\langle Q_i \rangle^{II} = \langle Q_7 \rangle \frac{\alpha_s(\mu_h) C_F}{4\pi} H_i$$

$$H_1^V(s) = -\frac{2\pi^2}{3N} \frac{f_B f_V^\perp}{F_V m_B^2} \underbrace{\int_0^1 d\xi \frac{\Phi_{B1}(\xi)}{\xi}}_{=: m_B/\lambda_B} \int_0^1 dv h(\bar{v}, s) \Phi_\perp^V(v)$$



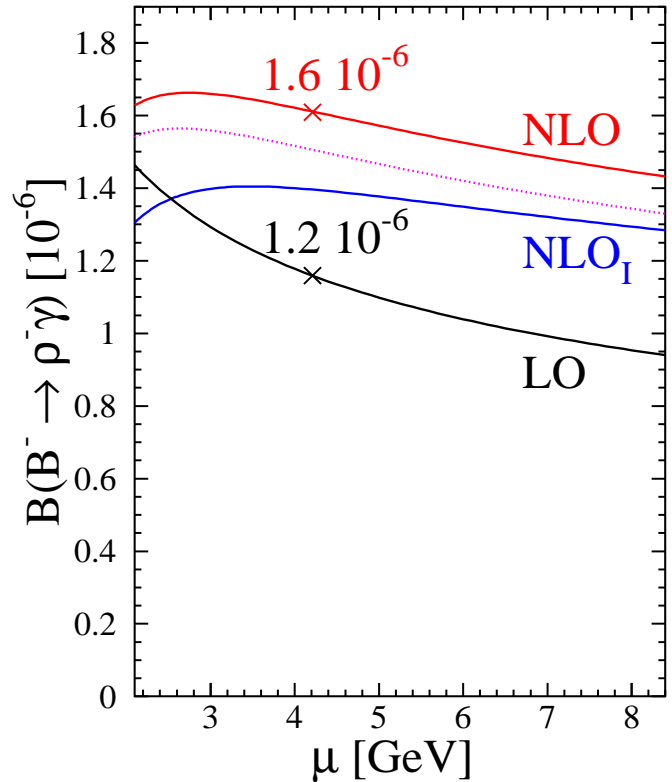
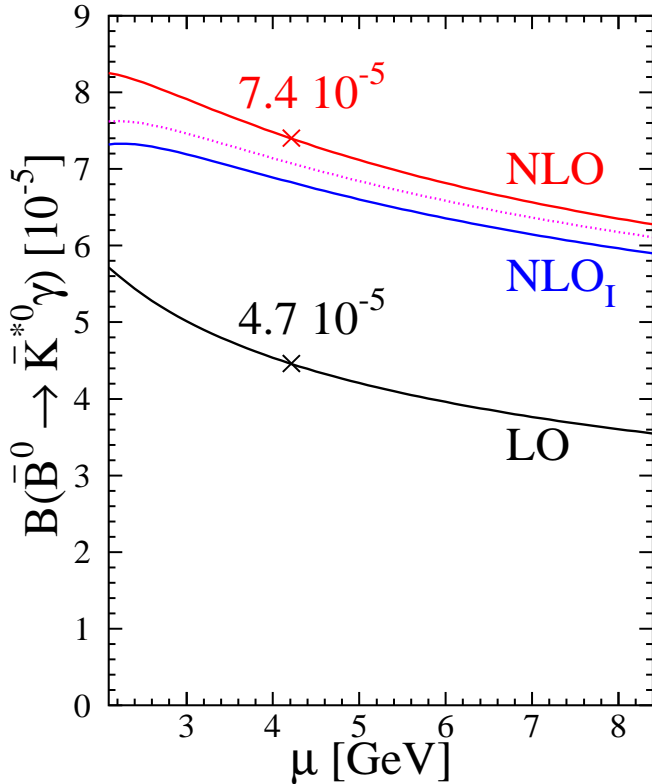
$$H_8^V = \frac{4\pi^2}{3N} \frac{f_B f_V^\perp}{F_V m_B^2} \int_0^1 d\xi \frac{\Phi_{B1}(\xi)}{\xi} \underbrace{\int_0^1 dv \frac{\Phi_\perp^V(v)}{v}}_{=3(1-\alpha_1^\perp+\alpha_2^\perp)}$$

# Results

$$A(\bar{B} \rightarrow V\gamma) = \frac{G_F}{\sqrt{2}} \left[ \sum_{p=u,c} \lambda_p^{\text{CKM}} a_7^p \right] \langle V\gamma | Q_7 | \bar{B} \rangle$$

$$a_7^p(V\gamma) = C_7 + \frac{\alpha_s(\mu)C_F}{4\pi} \sum_{i=1}^8 C_i(\mu)G_i(s) + \frac{\alpha_s(\mu_h)C_F}{4\pi} \sum_{j=1}^8 C_j(\mu_h)H_j^V$$

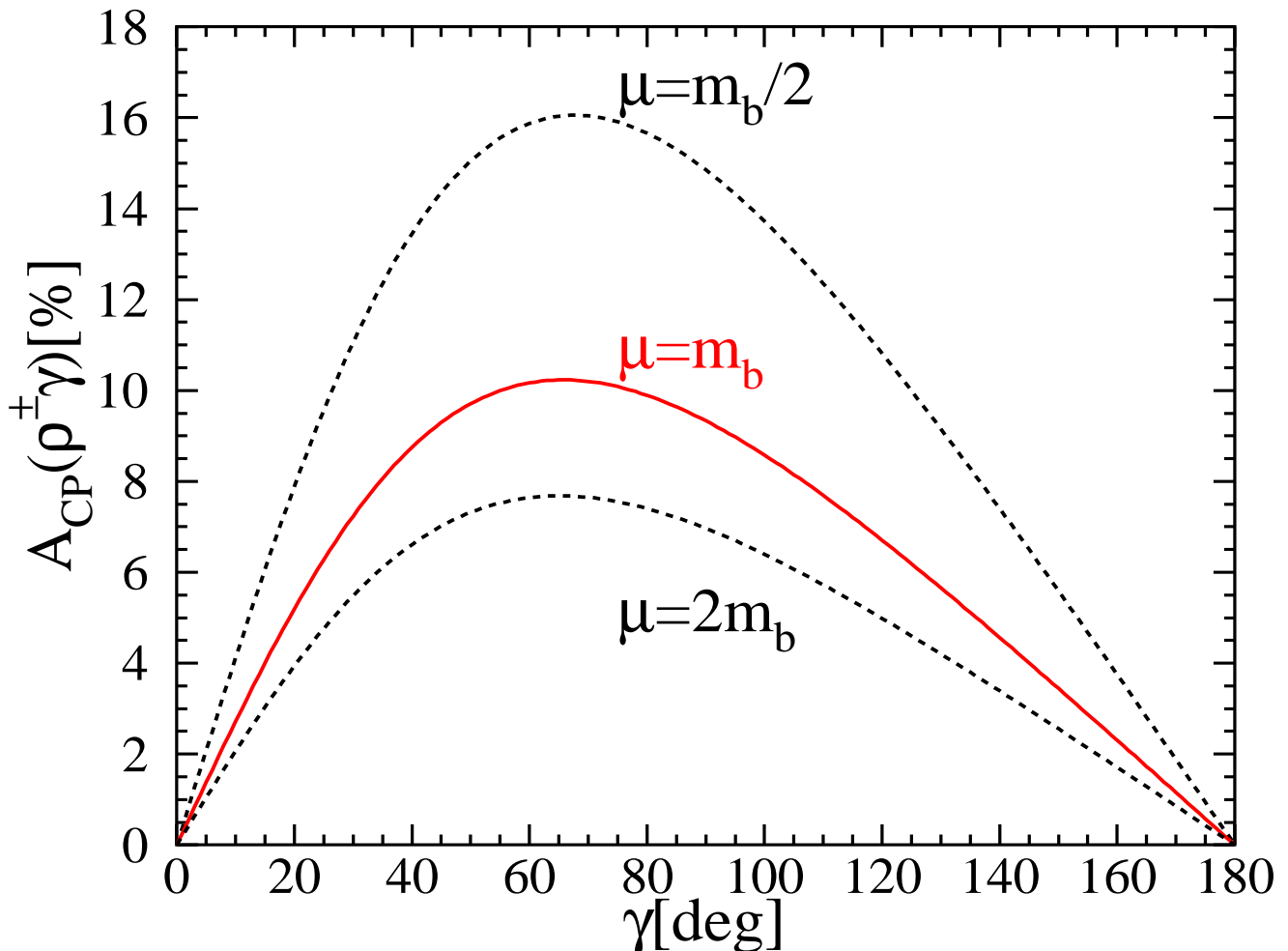
$$\begin{aligned} a_7^c(K^*\gamma) &= -0.322 + 0.011 \\ &\quad -0.079 - 0.013i \\ &\quad -0.017 - 0.012i \\ &= -0.407 - 0.025i \end{aligned}$$



# $B \rightarrow \rho\gamma$ Phenomenology

CP asymmetry

$$\begin{aligned} \mathcal{A}_{CP}(\rho\gamma) &= \frac{\Gamma(B \rightarrow \rho\gamma) - \Gamma(\bar{B} \rightarrow \rho\gamma)}{\Gamma(B \rightarrow \rho\gamma) + \Gamma(\bar{B} \rightarrow \rho\gamma)} \\ &\approx \frac{2 \operatorname{Im}\lambda_u^* \lambda_c}{|\lambda_t|^2} \frac{\operatorname{Im}a_7^{u*} a_7^c}{|C_7|^2} \end{aligned}$$



Maximum at  $\gamma \approx 65$  deg.

$$\mathcal{A}_{CP}(K^{*0}\gamma) = -0.3\%$$

# Isospin breaking

$$\Delta_{+0} = \frac{\Gamma(B^+ \rightarrow \rho^+ \gamma)}{2\Gamma(B^0 \rightarrow \rho^0 \gamma)} - 1$$

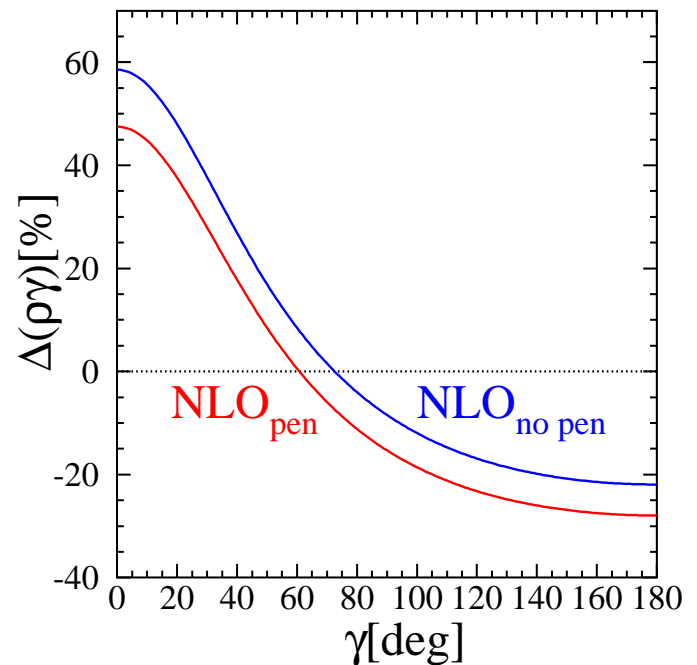
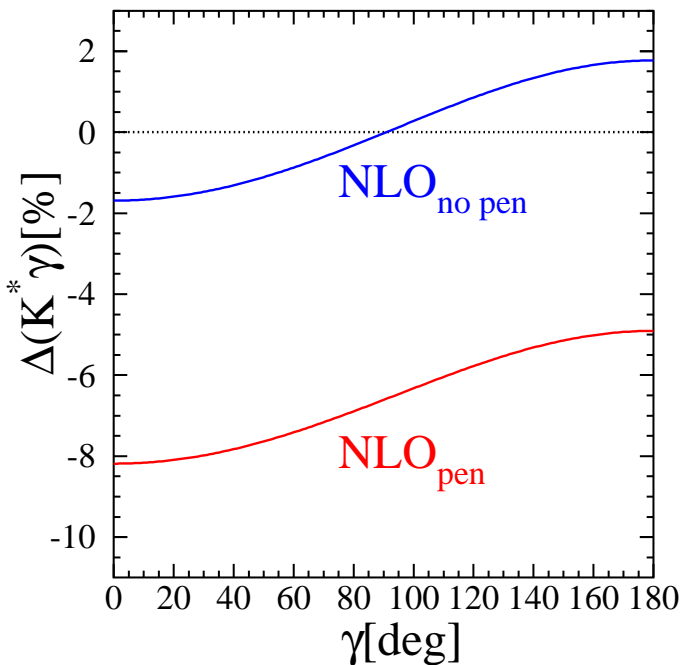
$$\Delta_{-0} = \frac{\Gamma(B^- \rightarrow \rho^- \gamma)}{2\Gamma(\bar{B}^0 \rightarrow \rho^0 \gamma)} - 1$$

$$\Delta(V\gamma) = \frac{\Delta_{+0} + \Delta_{-0}}{2}$$

Ali, Handoko, London  
SWB, Buchalla

large effect from  $Q_6$  on  $\Delta(K^* \gamma)$

Kagan, Neubert



$$\Delta(K^* \gamma) = (-7.5^{+4.1}_{-5.9})\% \quad \Delta(\rho \gamma) = (2.0^{+27.0}_{-15.7})\%$$

$$\Delta(K^* \gamma)_{\text{exp}} = (-19.2 \pm 11.8)\%$$



# Summary

- **systematic** and **model-independent** framework for rare radiative decays  $B \rightarrow V\gamma$  and  $B \rightarrow \gamma\gamma$
- **power counting** in the **heavy quark limit**
- **quark-loop** contributions **calculable** in **QCD factorization**
- non-factorizable **LD** corrections **power-suppressed**
- **strong phases** from spectator interaction important for **CP asymmetry**
- weak **annihilation** in  $B \rightarrow V\gamma$  **power suppressed** but numerically enhanced and **calculable**
- NLL:  $B(\bar{B}^0 \rightarrow \bar{K}^{*0}\gamma) = (7.4_{-2.4}^{+2.6}) \cdot 10^{-5}$   
 $B(B^- \rightarrow \rho^-\gamma) = (1.6_{-0.5}^{+0.7}) \cdot 10^{-6}$   
 $\mathcal{A}_{CP}(\rho^\pm\gamma) \sim 10\%$
- LL:  $B(\bar{B}_s \rightarrow \gamma\gamma) = (1.2_{-0.7}^{+2.5}) \cdot 10^{-6}$   
 $B(\bar{B}_d \rightarrow \gamma\gamma) = (3.1_{-2.1}^{+6.7}) \cdot 10^{-8}$
- dominant **uncertainty**: **non-perturbative** input **parameters** (form factors, decay constants,  $\lambda_B$ )